AN ADAPTIVE TRACKING ALGORITHM OF LUNG TUMORS IN FLUOROSCOPY USING ONLINE LEARNED COLLABORATIVE TRACKERS

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ABSTRACT

Accurate tracking of tumor movement in fluoroscopic video sequences is a clinically significant and challenging problem. This is due to blurred appearance, unclear deforming shape, complicate intra- and inter-fractional motion, and other facts. Current offline tracking approaches are not adequate because they lack adaptivity and often require a large amount of manual labeling. In this paper, we present a collaborative tracking algorithm using asymmetric online boosting and adaptive appearance model. The method was applied to track the motion of lung tumors in fluoroscopic sequences provided by radiation oncologists. Our experimental results demonstrate the advantages of the method.

Index Terms— Online Learning, Contour Tracking, Fluoroscopy.

1. INTRODUCTION

Accurate tracking of tumor movement in fluoroscopic video sequences is a clinically significant and challenging problem. The issue of precise target positioning of tumors in lung cancer is complicated by intra-fraction target motion. It has been well demonstrated that tumors located in the thorax may exhibit significant respiratory induced motions [1]. These physiologically related motions may increase the target positioning uncertainty and have a two-fold of impact on radiation treatment. First, the motions will blur the images and increase the uncertainty and have a two-fold of impact on radiation treatment. On the other hand, this increased uncertainty may unnecessarily include some normal tissues, which may lead to higher than expected normal tissue damage.

Recent computer-aided methods for tracking the tumor can be categorized into three groups: (1) Finding the tumor positions based on the external surrogates [2]; (2) Tumor tracking with the help of fiducial markers inside or near the tumor [3]; (3) Tumor tracking without implanted fiducial markers. The optical flow [4] produces promising tracking results when there is relatively small motion between adjacent frames. Respiration motion also complicates accurate tracking of tumors making it necessary to apply adaptive trackers. Shape models of individual annotated tumors at different phases of respiration were learned offline to achieve good tracking results [5]. A motion model and one step forward prediction were applied to reliably track the left ventricle in 3D ultrasound [6]. However, these methods require a lot of expensive annotations and can only track tumors by utilizing learned shape priors or motion priors.

In this paper, we present an adaptive tracking algorithm of lung tumors in fluoroscopic image sequences using online learned collaborative trackers. Through the use of online updating, our method does not require large number of manual annotations and can adjust to appearance changes adaptively. Adaptive classifiers are "taught" to discriminate landmark points in the contour from others. They are incrementally updated during the whole tracking process. Appearance of the local window centered in each landmark point is modeled in a low dimensional subspace. The algorithm was evaluated using two fluoroscopic sequences of lung cancer provided by radiation oncologists.

2. ONLINE CONTOUR TRACKING

The tumor contour is represented as a list of landmark points in clockwise order. We denote the contour as \( C = \{c_1, c_2, ..., c_n\} \), where \( c_i \) is the \( i \)-th landmark point. Let \( Z = \{z_1, z_2, ..., z_n\} \) as the observation of the contour, \( \Lambda = \{\chi_1, \chi_2, ..., \chi_n\} \) as the states of the contour, and \( \chi_i = \{x, y\} \) is the coordinates of landmark point \( c_i \). The tracking problem can be represented as the estimation of a state probability \( p(\Lambda_t | Z_{1:t}) \), where \( Z_t \) is the observation at the \( t \)-th frame.

\[
p(\Lambda_t | Z_{1:t}) \propto p(Z_t | \Lambda_t)p(\Lambda_{t-1} | Z_{1:t-1}) \tag{1}
\]

\( \Lambda^*_t = \arg \max_\Lambda p(\Lambda_t | Z_{1:t}) \) is the estimation of the contour tracking result.

Assuming each landmark point is independent from each other, let \( \chi_i \) and \( z_i \) serve as the state and observation of the
i-th landmark point in the t-th frame. Then (1) is equivalent to:

\[ p(A_t|Z_{1:t}) \propto \prod_{i=1}^{n} p(\chi_t, z_1, z_2, ..., z_t). \]  

(2)

Tracking results for all landmark points with a maximum \( p(\chi_t, z_1, z_2, ..., z_t) \) yield the optimal solution of (2). For convenience, we present the contour tracking as the estimation of \( p(\chi_t|z_{1:t}) \) for each point. Bayesian importance sampling estimates and propagates the probability by recursively performing prediction:

\[ p(\chi_t|z_{1:t-1}) = \int p(\chi_t|\chi_{t-1})p(\chi_{t-1}|z_{1:t-1})d\chi_{t-1} \]  

(3)

and updating

\[ p(\chi_t|z_{1:t}) \propto p(\chi_t|\chi_{t-1})p(\chi_{t-1}|z_{1:t-1}). \]  

(4)

The transition model \( p(\chi_t|\chi_{t-1}) \) is constrained by assuming a Gaussian distribution \( N(\chi_t|\chi_{t-1}, \sigma) \). The observation model \( p(z_t|\chi_t) \) represents the likelihood of \( z_t \) being generated from state \( \chi_t \). In our algorithm, it is measured with two independent models collaboratively. One is a discriminative model using an asymmetric online updated classifier. The other is based on a generative model, which represents the appearance of each small region around the landmark point in an incrementally learned low dimensional subspace. For point observation \( z_t \) in the current frame, the observation model is

\[ p(z_t|\chi_t) \propto p_D(z_t|\chi_t)p_G(z_t|\chi_t), \]  

(5)

where \( p_D(z_t|\chi_t) \) and \( p_G(z_t|\chi_t) \) are the likelihood calculated from the discriminative and generative models, respectively. Substituting (5) into (4), the point tracking result \( \chi_t = \text{argmax}_{\chi_t} p(\chi_t|z_{1:t}) \).

3. ASYMMETRIC ONLINE BOOSTING

We define training samples \( \{x_i\}_{i=1}^{N} \in R^d \) and their labels \( \{y_i\}_{i=1}^{N} \in \{-1, 1\} \), where \( y = 1 \) denotes a landmark point and \( y = -1 \) is a background point. A function \( f(x) : R^d \rightarrow R \) can be learned as the confidence of labeling sample \( x \). \( x \) is classified to be the object if \( f(x) > 0 \) or background otherwise. The \( p_D(z_t|\chi_t) \) in (5) is measured by \( f(x) \), where \( x \) is the sample generated with state \( \chi_t \). Because the training samples are unbalanced and provided incrementally, the discriminative model is trained using asymmetric online boosting. This method provides a more robust classifier and converges faster for unbalanced training sets [7].

Boosting constructs a strong classifier as a linear combination of \( T \) weak classifiers \( h_i(x) \in \{-1, 1\} \) where \( i = 1, 2, ..., T \):

\[ H(x) = \text{sign}(f(x)), \]  

(6)

\[ f(x) = \sum_{i=1}^{T} \alpha_i h_i(x). \]  

(7)

**Algorithm 1:** Asymmetric online boosting

**Define:** Let \( \{x_i, y_i\}_{i=1}^{N} \) represent the dataset, \( x_i = \{x_{i1}, ..., x_{id}\} \) is \( d \) dimensional feature vector and \( y_i \in \{-1, 1\} \) is its label. The \( \gamma \) is the learning rate. \( \omega = \{\omega_1, \omega_2, ..., \omega_N\} \) is the samples’ weight. The \( H_t(x) \) is the strong classifier in the \( t \)-th iteration with confidence function \( f_t(x) \), the weighted accuracy and error are denoted as \( \lambda_{m} \) and \( \lambda_{m}^{\text{wor}} \), \( m = 1, ..., M \), where \( M \) is number of weak classifiers in the pool. The \( I \) is the indicator function.

1. \( \omega_i = 1, i = 1, ..., N \)
2. for \( t = 1, 2, ..., T \) do
3. \( \omega_i = \omega_i \exp(y_i \sqrt{E}/T) \)
4. \( \omega_i = \omega_i / \sum_{j=1}^{N} \omega_j \)
5. for \( m = 1, 2, ..., M \) do
6. \( h_m(x) = \text{update}(h_m(x), \{x_i, y_i\}_{i=1}^{N}, \omega) \)
7. \( \lambda_{m} = \lambda_{m}^{\text{cor}}(1-\gamma) + \gamma \sum_{i=1}^{N} \omega_i I(h_m(x_i) = y_i) \)
8. \( \lambda_{m}^{\text{wor}} = \lambda_{m}^{\text{cor}}(1-\gamma) + \gamma \sum_{i=1}^{N} \omega_i I(h_m(x_i) \neq y_i) \)
9. \( \epsilon_m = \lambda_{m}^{\text{wor}}/(\lambda_{m}^{\text{cor}} + \lambda_{m}^{\text{cor}}) \)
10. end for
11. \( m^* = \text{argmin}_{m} \epsilon_m \)
12. \( \alpha_t = \frac{1}{2} \log(\frac{1-\epsilon_{m^*}}{\epsilon_{m^*}}) \)
13. \( \omega_i = \omega_i \exp(-y_i \cdot h_{m^*}(x_i)) \)
14. \( f_t(x) = f_{t-1}(x) + \alpha_t h_{m^*}(x) \)
15. \( H_t(x) = \text{sign}(f_t(x)) \)
16. end for

The weight \( \alpha_t \) of \( h_t(x) \) is correlated to its classification accuracy on the training data. However, good performance of the standard Adaboost requires a large and balanced training set. We have a limited amount of labeled training samples, and the number of positive samples is much lower than the number of negative samples. Instead of weighting positive and negative samples evenly, we force the penalty of a false negative to be \( k \) times larger than a false positive. Compared with the standard loss function \( \exp(-y_i \cdot H_t(x_i)) \) defined in Adaboost, the loss function in our algorithm is:

\[ \epsilon(H) = \mathbb{E}(A\text{Loss}(H(x), y)), \]  

(8)

where

\[ A\text{Loss}(H(x), y) = \begin{cases} 
    k_1^{1/2} & \text{if } y = 1, H(x) = -1 \\
    k_2^{-1/2} & \text{if } y = -1, H(x) = 1 \\
    0 & \text{otherwise}
\end{cases}, \]  

(9)

which is proven to be effective in [7]. This asymmetric loss function can be integrated into an online boosting algorithm by multiplying the original weights \( \exp(-y_i \cdot H_t(x_i)) \) with \( \exp(y_i \sqrt{E}) \). For an online boosting algorithm with \( T \) iterations, samples are weighted by times \( \exp(y_i \sqrt{E}/T) \) at each
iteration to avoid the asymmetric weights to be absorbed by the first selected weak learner.

The asymmetric online boosting method used in our algorithm is summarized in Algorithm (1). The strong classifier \( H(x) \) is updated incrementally using tracking results in the current frame. Each weak learner \( \hat{h}_i(x) \) and its corresponding weight \( \alpha_i \) are updated with learning rate \( \gamma \) (shown in Algorithm (1)). This online updating schema enabled the incrementally trained classifier to be more adaptive to gradual appearance changes.

4. DYNAMIC APPEARANCE MODEL AND SUBSPACE LEARNING

The online boosting classifier utilizes a limited number of online selected weak learners with best discriminative power. However, it is still challenging to discriminate landmarks with similar appearance, which are very common in fluoroscopic images. Dynamic appearance model handles this challenge by learning the target incrementally.

Without losing generality, we define \( I = (I_1, I_2, \ldots, I_n) \) as \( n \) observations of one landmark point in \( n \) consecutive frames, \( I \) can be modeled as a space spanned by low dimensional orthogonal subspace \( U_{q,k} \) centered at \( \mu \), where \( q \) is the length of the vectorized model and \( k \) is the dimension of the subspace. The \( U \) is the low dimension eigenvectors of the samples’ covariance matrix \( \frac{1}{n} \sum_{i=1}^{n} (I_i - \mu)(I_i - \mu)^T \), and \( \mu = \frac{1}{n} \sum_{i=1}^{n} I_i \) is the moving average.

Let \( \Omega = \{ \mu, U, \Sigma \} \) serves as the appearance model for \( I \), \( \Sigma \) is a diagonal matrix contains \( k \) largest ordered singular values of \( I \) and \( \lambda_1 > \lambda_2 > \cdots > \lambda_k \). For a given sample \( I_{\chi_i} \) extracted in state \( \chi_i \), the likelihood of \( I_{\chi_i} \) generated from the model \( \Omega \) can be decomposed into the probabilities of distance-within-subspace [8],

\[
p_U(I_{\chi_i} | \Omega) \propto \exp\left(-\frac{1}{2}(I_{\chi_i} - \mu)^T U \Sigma^{-2} U^T (I_{\chi_i} - \mu)\right),
\]

(10)

and distance-to-subspace,

\[
p_U(I_{\chi_i} | \Omega) \propto \exp(-||I_{\chi_i} - \mu - UU^T (I_{\chi_i} - \mu)||^2).
\]

(11)

The generative model \( p_G \) in (5) is estimated as

\[
p_G(z_t|\chi_t) = p_U(I_{\chi_i} | \Omega)p_G(I_{\chi_i} | \Omega).
\]

(12)

Let \( A \) denote the observations in the previous \( n \) frames and \( B \) represent the most recent \( m \) frames. Incremental subspace learning [8] is performed to merge the new frames into the original subspace learned from \( A \). With \( A = U \Sigma V^T \) by singular value decomposition (SVD), \( B \) as the concatenated centered data of \( B \) plus one additional vector \( \sqrt{\frac{m}{n+m}} (\mu_B - \mu) \), and \( \hat{B} \) as the components of \( \hat{B} \) orthogonal to \( U \), the concatenated matrix of \( A \) and \( B \) then can be written as

\[
[A \ B] \equiv [U \ \hat{B}]R \begin{bmatrix} V^T & 0 \\ 0 & I \end{bmatrix},
\]

(13)

where \( R = \begin{bmatrix} \Sigma & U^T \hat{B} \\ 0 & \hat{B}(\hat{B} - UU^T \hat{B}) \end{bmatrix} \). After we calculate the SVD of \( R = \hat{U} \Sigma \hat{V}^T \), the new subspace is updated as \( \hat{U'} = [U \ \hat{B}] \hat{U} \) and \( \hat{\Sigma'} = \hat{\Sigma} \). The mean \( \mu' = \frac{n}{n+m} \mu_A + \frac{m}{n+m} \mu_B \) is updated with a forgetting factor \( \gamma \) to decrease the weight of the older appearance models.

5. EXPERIMENTAL RESULTS

Two sets of fluoroscopic video sequences on a patient were collected to test our algorithm. The fluoroscopic images were acquired for a consented lung cancer patient who had right hilar T2 stage non-small cell lung cancer and was undergoing radiotherapy. These fluoroscopic images were saved in digital format and readily available for video display and analysis. Each sequence lasts for about 10 seconds and covers two to three respiration cycles. The first set is a posterior-anterior (PA) fluoroscopic video sequence, and the second one is a lateral sequence. As discussed previously, the quantified moving information is extremely important in radiotherapy management of lung cancers. Using the prescribed algorithm, an optimal plan and treatment strategy can be designed to provide a desired conformal dose coverage to a tumor target while sparing as much surrounding normal tissues as possible.

The experiments of the algorithm were conducted as follows. The initial contours for these sequences were labeled in a 3D CT by an experienced radiation oncologist. On the 3D CT images, the target (cancer tumor) could be clearly identified and delineated. Digitally reconstructed radiograph, along with the delineated contours, were projected along the PA and lateral directions. Based on the digitally reconstructed radiograph and projected target, an experienced radiation oncologist manually identified and delineated the target in the first frame of each fluoroscopic video sequence. The tracking procedure was then started automatically. The results are shown in Figure 1. Sequence 1 contains 223 frames and the results of frame (4, 74, 144, 214) are displayed in Figure 1a. Sequence 2 contains 120 frames and the results of frame (2, 42, 82, 120) are displayed Figure 1b. The tracking results were compared with point tracking by optical flow using a 40 \times 40 window. Although each sequence exhibits different illumination and contrast changes due to different acquisition directions, the algorithm we presented can provide a reasonably accurate tracking result of the tumors. The comparative experiments demonstrated that our algorithm outperforms optical flow.

6. CONCLUSION

We have proposed an adaptive tracking algorithm for lung tumors in fluoroscopy using online learned collaborative trackers. No shape or motion priors are required for this tracking algorithm. This saves many expensive expert annotations. The experimental results demonstrate the effectiveness of our method. Instead of building a specific model, all the major steps in our algorithm are based on online updating. This
adaptive online learning algorithm is therefore general to be extended to other medical tracking applications.

7. REFERENCES


